



THE UNIVERSITY OF TEXAS AT DALLAS

# Image Processing: Filtering

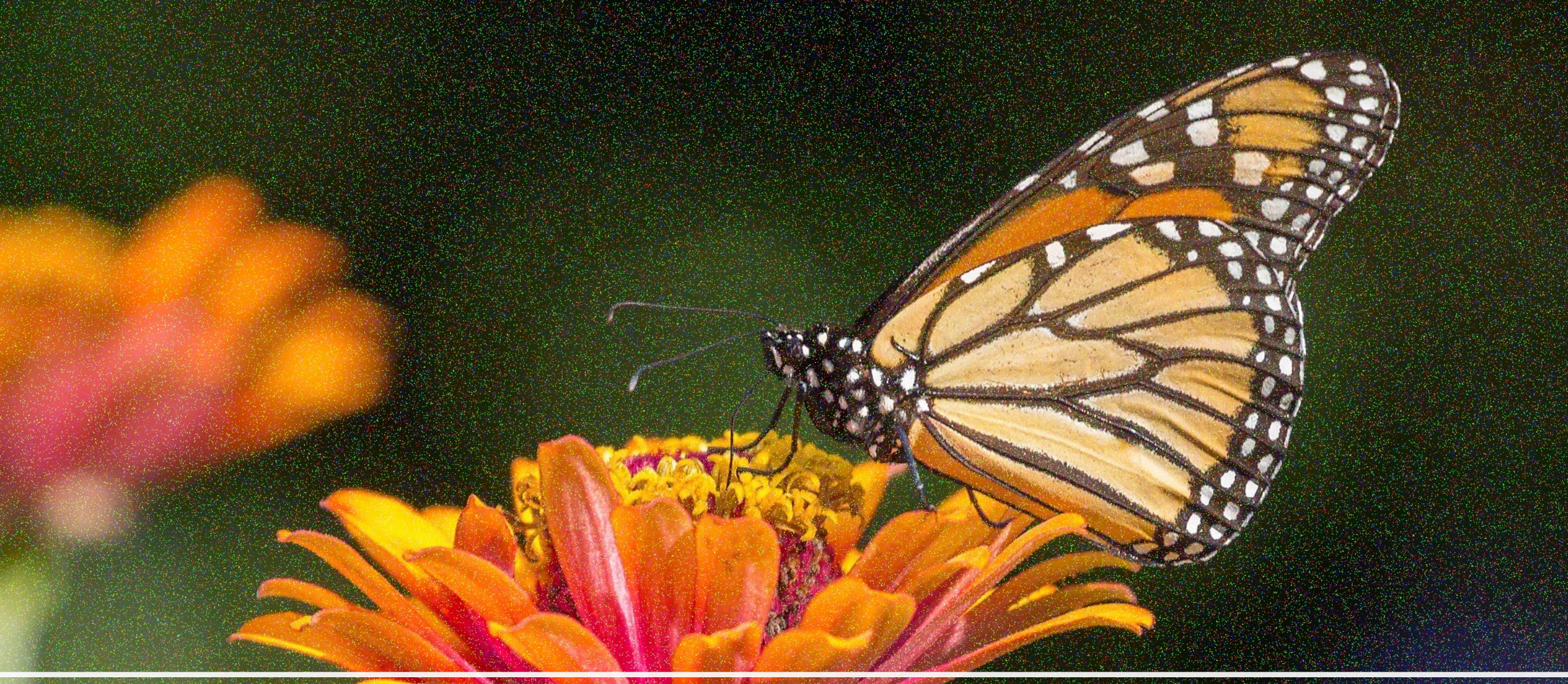
CS 6384 Computer Vision

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Department of Computer Science



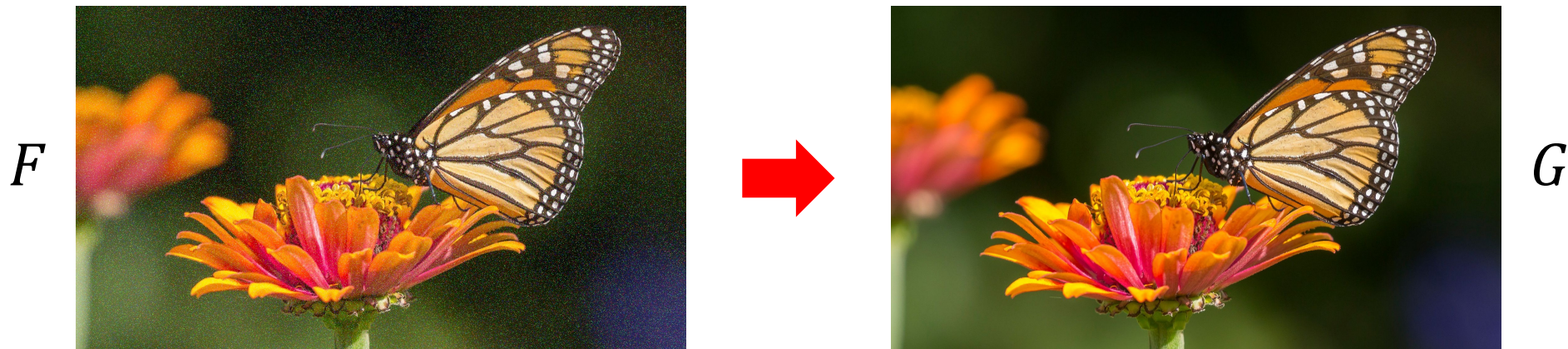




Question: How to reduce noises in an image?

# Image Filtering

- Goal: generate a new image  $G$  whose pixel values are a combination of the original pixel values  $F$ 
  - Enhance image quality (e.g., denoising, sharpening)
  - Extract visual features (e.g., edges, contours)
  - Basic computation unit in convolutional neural networks




# Noise Reduction as An Example

How was the noisy image generated?



$$F[i, j, c] = I[i, j, c] + n[i, j, c]$$

$i$  : row,  $j$ :column,  $c$ :color,  $n$ : additive noise

A monarch butterfly is perched on a vibrant orange and yellow flower. The background is dark and filled with a heavy, grainy noise, making the scene difficult to discern. The butterfly's wings are clearly visible, showing their characteristic orange and black patterns.

How to remove the noise  $n$  from the noisy image ?

# Characteristics of Noises and Natural Images

Image noises:

- **Random** and characterized by high frequency components
- Fewer details or finer textures

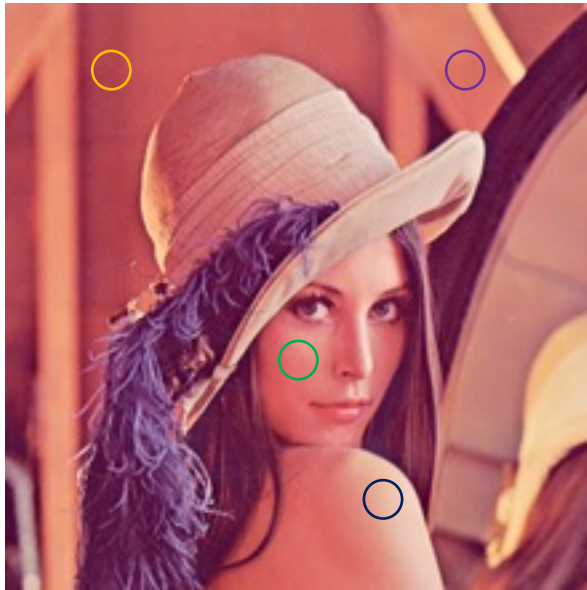
Natural images:

- Both low and high frequencies that are more evenly distributed
- More textures, patterns, and shapes with **gradual changes** in intensity or color



# Image Prior: Local Smoothness

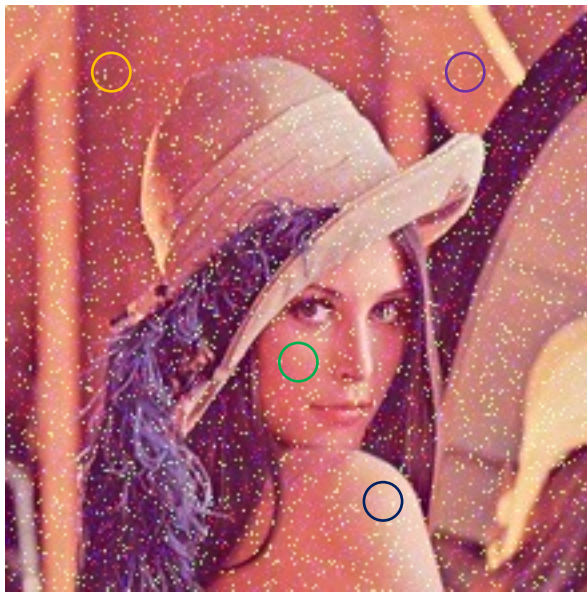
- Local natural image regions are typically smooth or uniform
- The overall structures or texture of a natural image often has a more subtle and gradual variation than image noise



- Image pixels in a small window (e.g., 5x5) usually are similar
- Noise values are dramatically changing at arbitrary directions

# Image Prior: Local Smoothness

- Local natural image regions are typically smooth or uniform
- The overall structures or texture of a natural image often has a more subtle and gradual variation than image noise

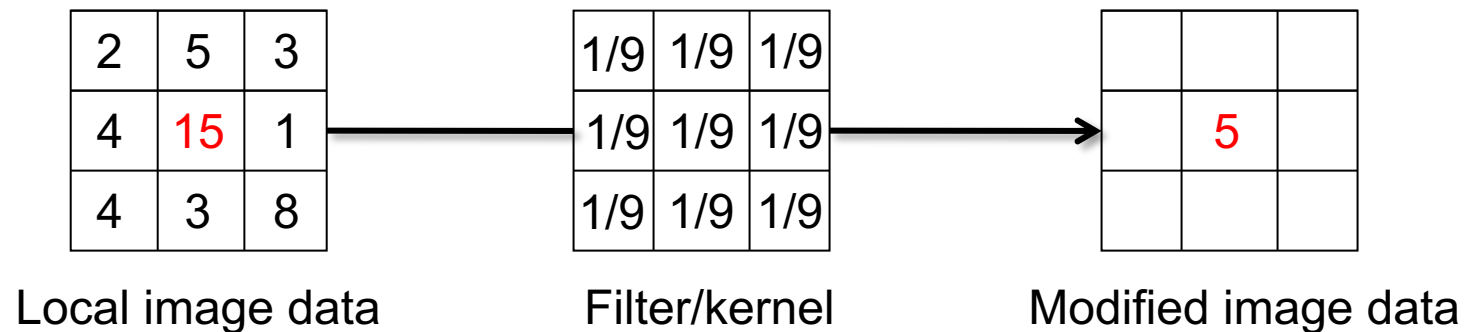


- Image pixels in a small window (e.g., 5x5) usually are similar
- Noise values are dramatically changing at arbitrary directions
- Due to noises, a noisy image have higher local variations than the clean image

# Image Filtering for Noise Reduction

Reduce noises by enforcing local smoothness prior

- Make each pixel in a noisy image to be similar to its local neighborhoods
- How? There are many local neighborhoods (e.g., 9 in a 3x3 window)
  - A naïve method: replace each pixel value with the mean value of its local neighborhoods



# Image Filtering Process

$1/9$	$1/9$	$1/9$
$1/9$	$1/9$	$1/9$
$1/9$	$1/9$	$1/9$



Noisy Image

Apply the filter to every pixel

# Image Filtering Process

$1/9$	$1/9$	$1/9$
$1/9$	$1/9$	$1/9$
$1/9$	$1/9$	$1/9$



Filtered Image

Apply the filter to every pixel



Filtered Image



Noisy Image

# Image Filtering

Modify the pixels in an image based on some function of a local neighborhood of each pixel

10	5	3
4	5	1
1	1	7

Local image data

Some function



	7	

Modified image data

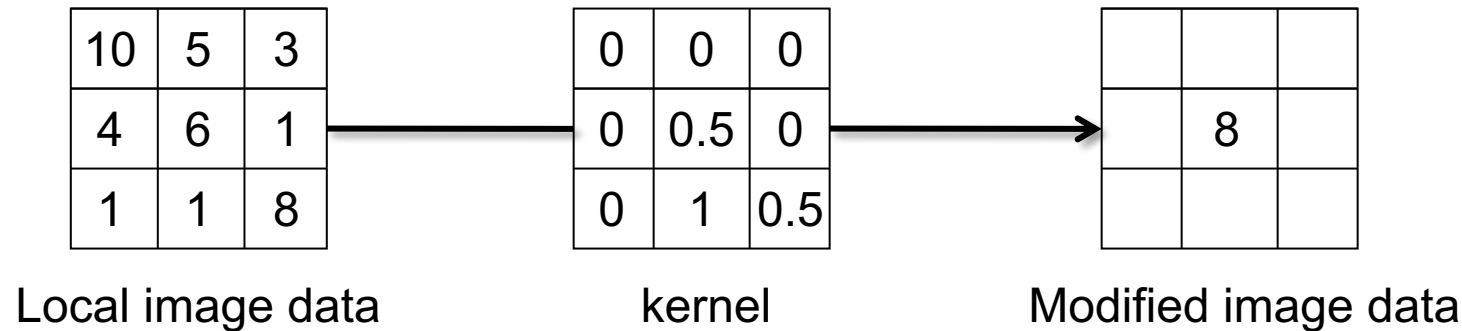
Slide credit: N. Snavely

# Linear filtering

A simple filtering: linear filtering (cross-correlation/convolution)

- Replace each pixel by a linear combination (a weighted sum) of its neighbors

The prescription for the linear combination is called the “kernel” (or “mask”, “filter”)



Slide credit: N. Snavely



# Cross-correlation

Let  $F$  be the image,  $H$  be the kernel (of size  $2k+1 \times 2k+1$ ), and  $G$  be the output image

$$G[i, j] = \sum_{u=-k}^k \sum_{v=-k}^k H[u, v] F[i + u, j + v]$$

This is called a **cross-correlation**

operation:  $G = H \otimes F$

Can think of as a “dot product” between local neighborhood and kernel for each pixel

Slide credit: N. Snavely

# Convolution

Same as cross-correlation, except that the kernel is “flipped” (horizontally and vertically)

$$G[i, j] = \sum_{u=-k}^k \sum_{v=-k}^k H[u, v] F[i - u, j - v]$$

This is called a **convolution** operation:

Convolution is **commutative** and **associative**

$$G = H * F$$

Slide credit: N. Snavely

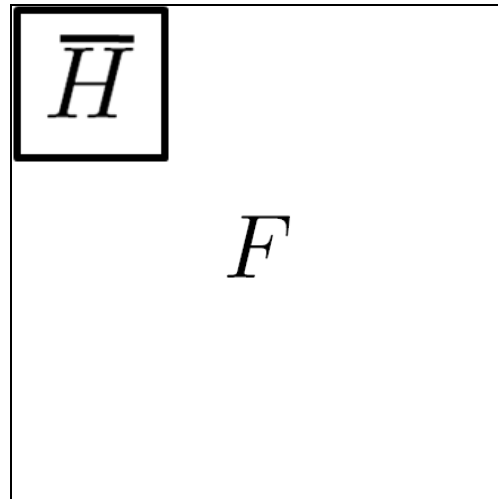
# Convolution



Kernel

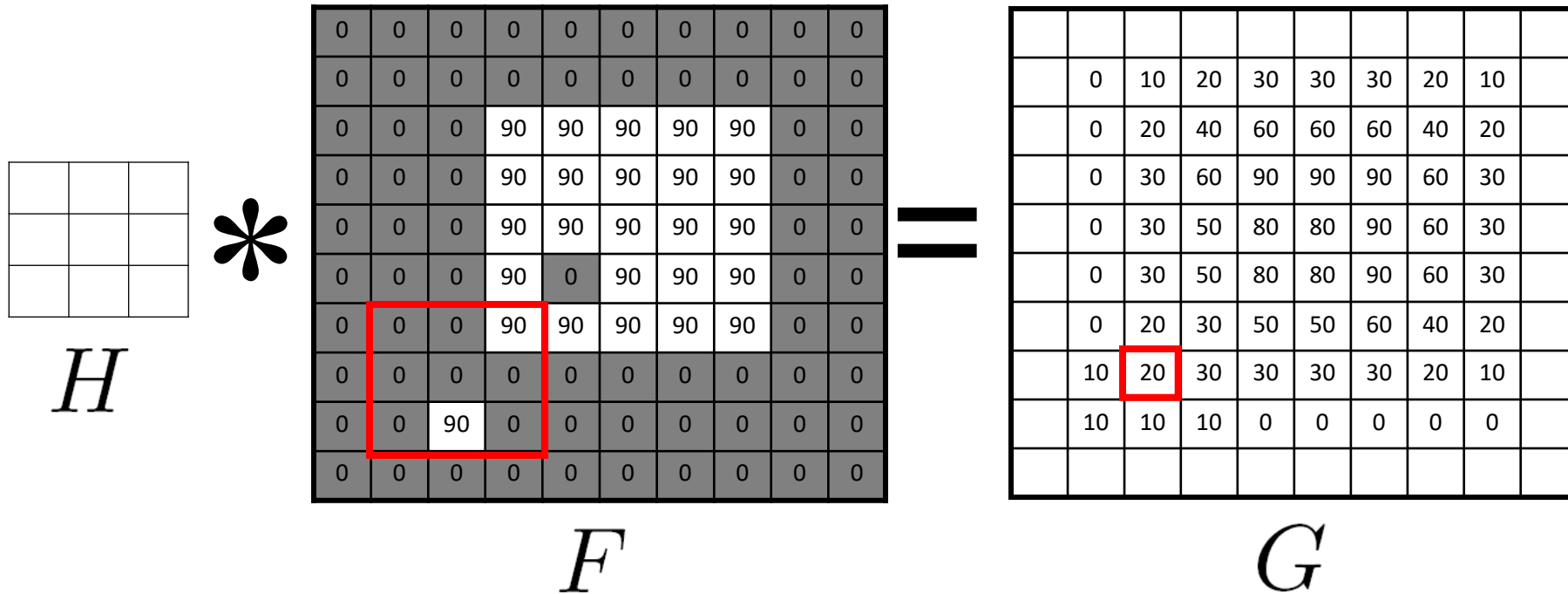


Flipped  
Kernel



Adapted from F. Durand

# Mean filtering



Slide credit: N. Snavely

# Mean filtering/Moving average

$F[x, y]$

0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	0	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0

$G[x, y]$


Slide credit: N. Snavely

# Mean filtering/Moving average

$F[x, y]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

$G[x, y]$

	0	10							

Slide credit: N. Snavely

# Mean filtering/Moving average

$F[x, y]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

$G[x, y]$

	0	10	20						

Slide credit: N. Snavely

# Mean filtering/Moving average

$$F[x, y]$$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

$$G[x, y]$$

	0	10	20	30					

Slide credit: N. Snavely



# Mean filtering/Moving average

$F[x, y]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

$G[x, y]$

	0	10	20	30	30				

Slide credit: N. Snavely

# Mean filtering/Moving average

$F[x, y]$

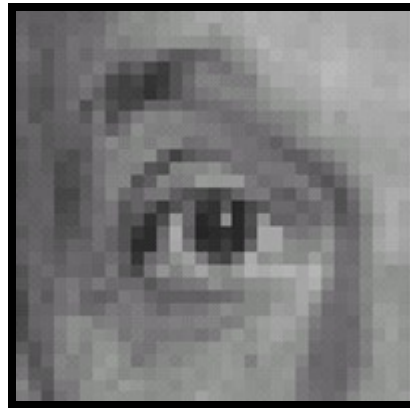
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

$G[x, y]$

	0	10	20	30	30	30	20	10	
	0	20	40	60	60	60	40	20	
	0	30	60	90	90	90	60	30	
	0	30	50	80	80	90	60	30	
	0	30	50	80	80	90	60	30	
	0	20	30	50	50	60	40	20	
	10	20	30	30	30	30	20	10	
	10	10	10	0	0	0	0	0	

Slide credit: N. Snavely

# Linear filters: examples



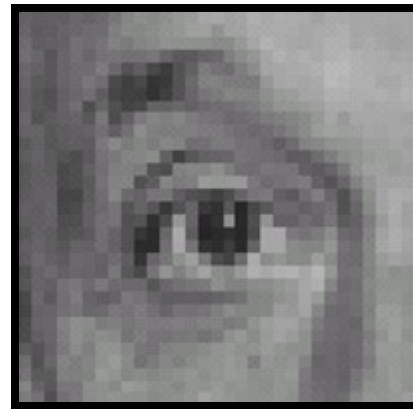
Original



0	0	0
0	1	0
0	0	0

Source: D. Lowe

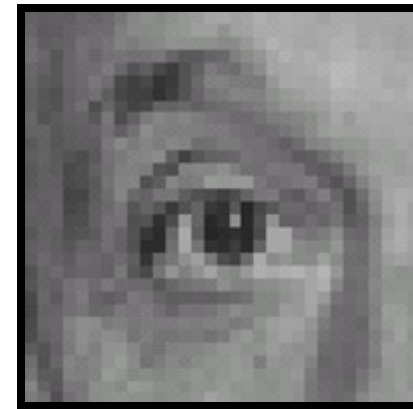
# Linear filters: examples



Original



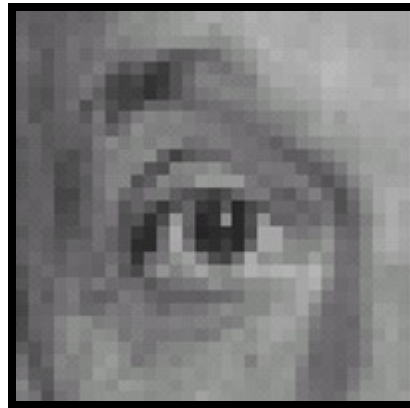
0	0	0
0	1	0
0	0	0



Identical image

Source: D. Lowe

# Linear filters: examples



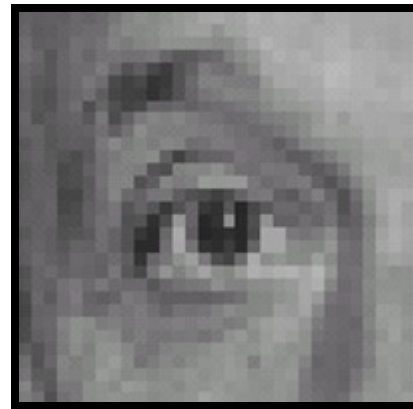
Original



0	0	0
1	0	0
0	0	0

Source: D. Lowe

# Linear filters: examples



Original



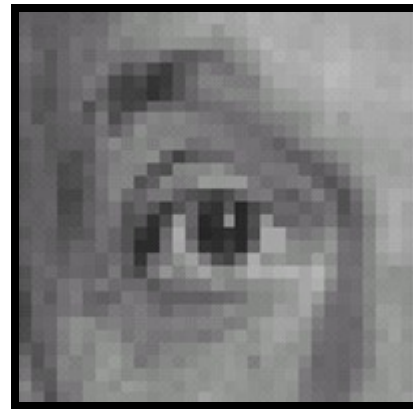
0	0	0
1	0	0
0	0	0



Shifted left by 1 pixel

Source: D. Lowe

# Linear filters: examples

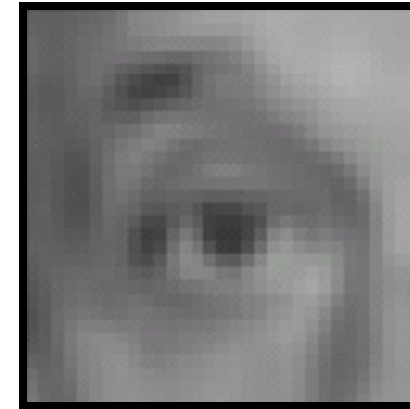


Original



$\frac{1}{9}$

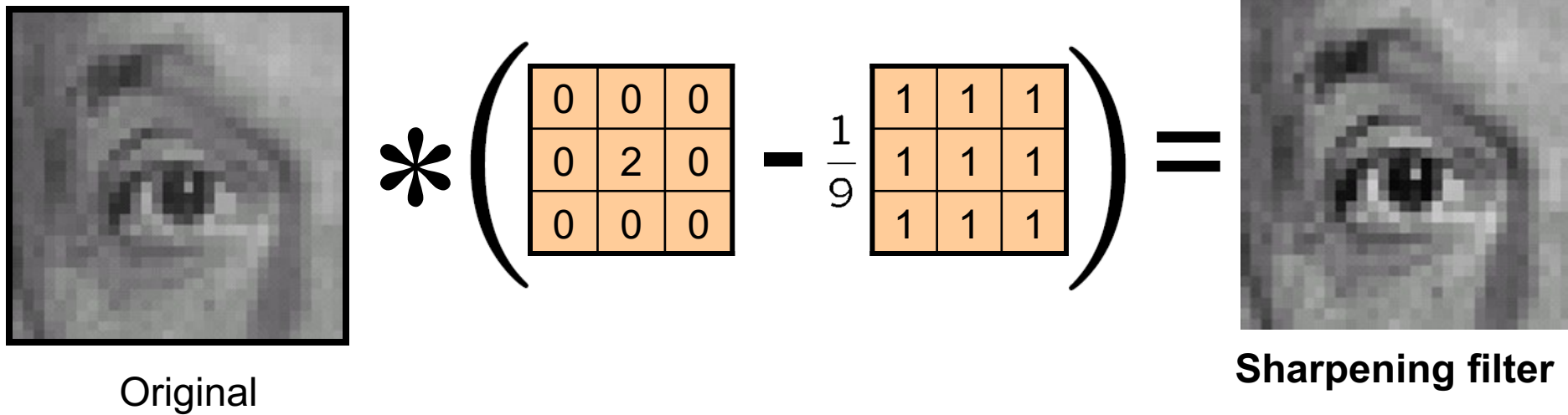
1	1	1
1	1	1
1	1	1



Blur (with a mean/box filter)

Source: D. Lowe

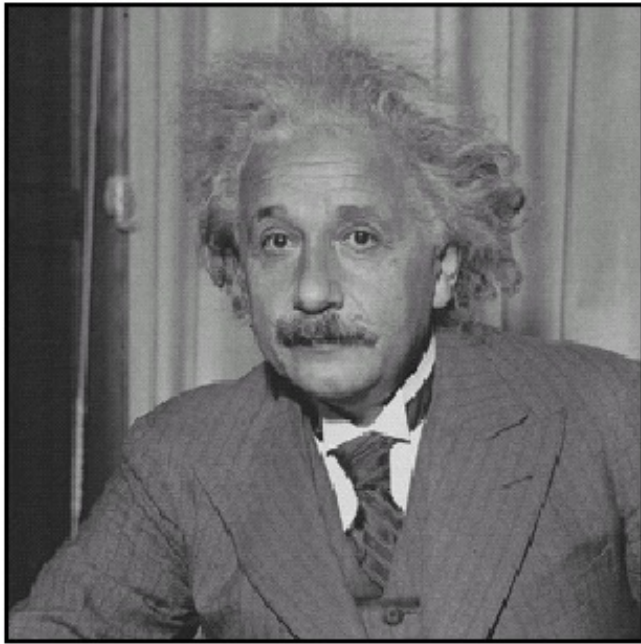
# Linear filters: examples



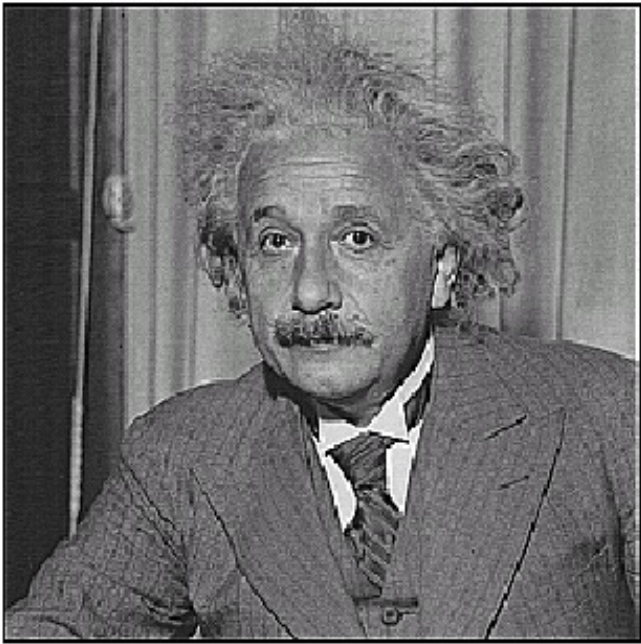
Source: D. Lowe



# Sharpening



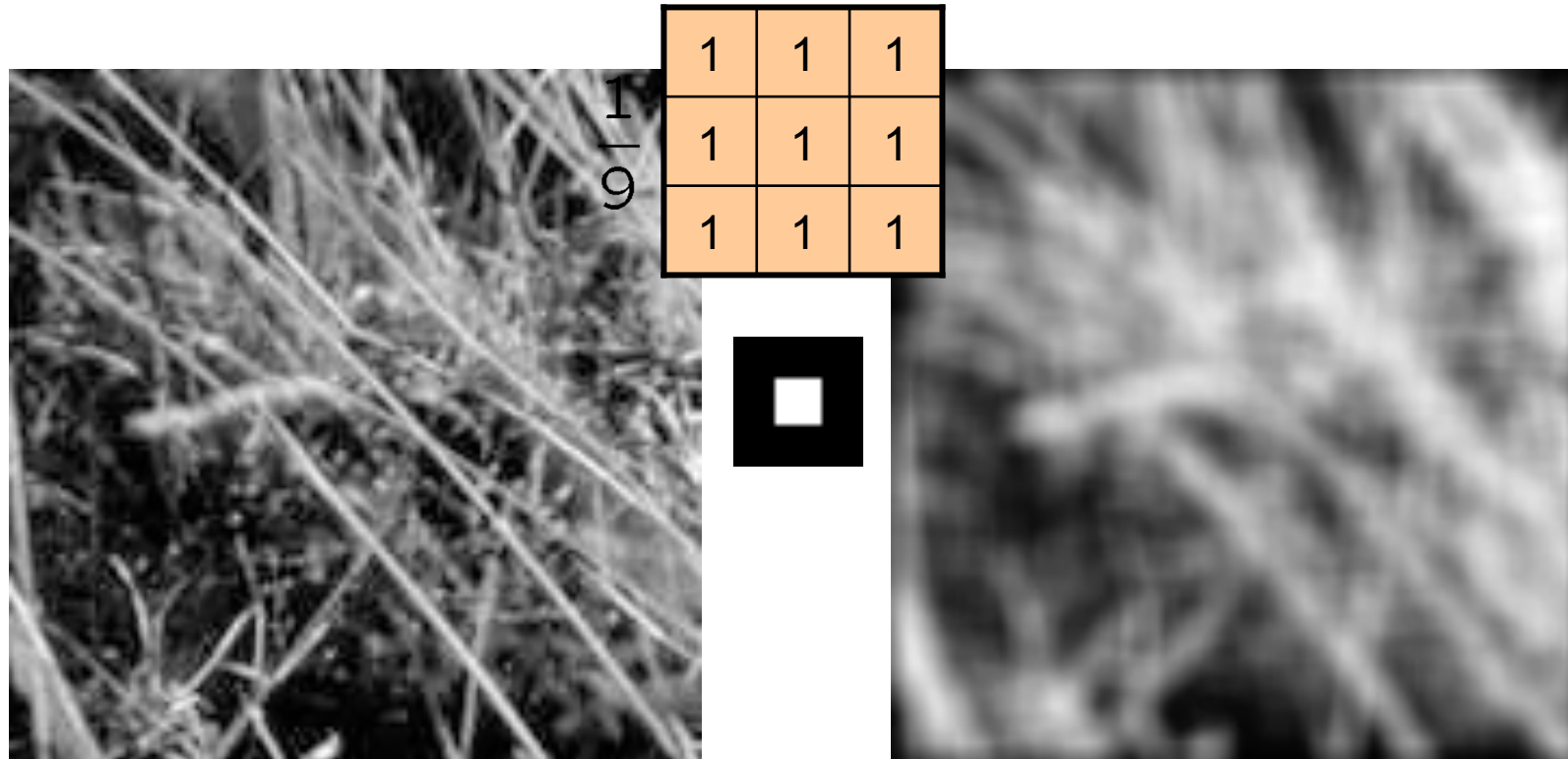
before



after

Source: D. Lowe

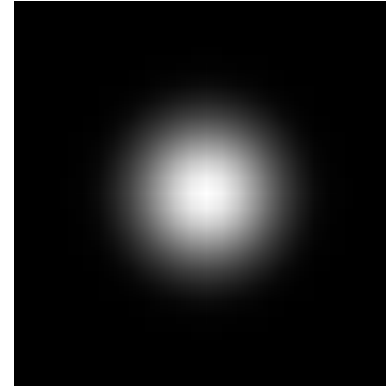
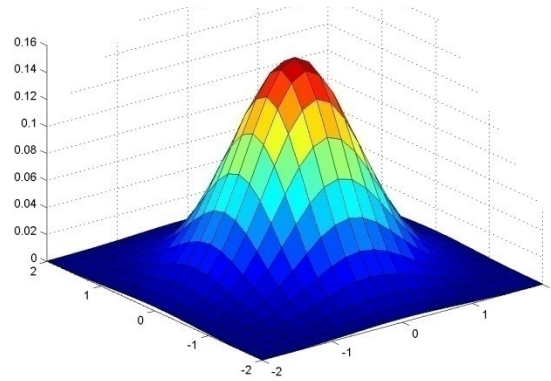
# Smoothing with mean filter revisited



Block artifacts appear in the outputted image because non-relevant pixels are assigned the same weights during filtering

Source: D. Forsyth

# Gaussian kernel

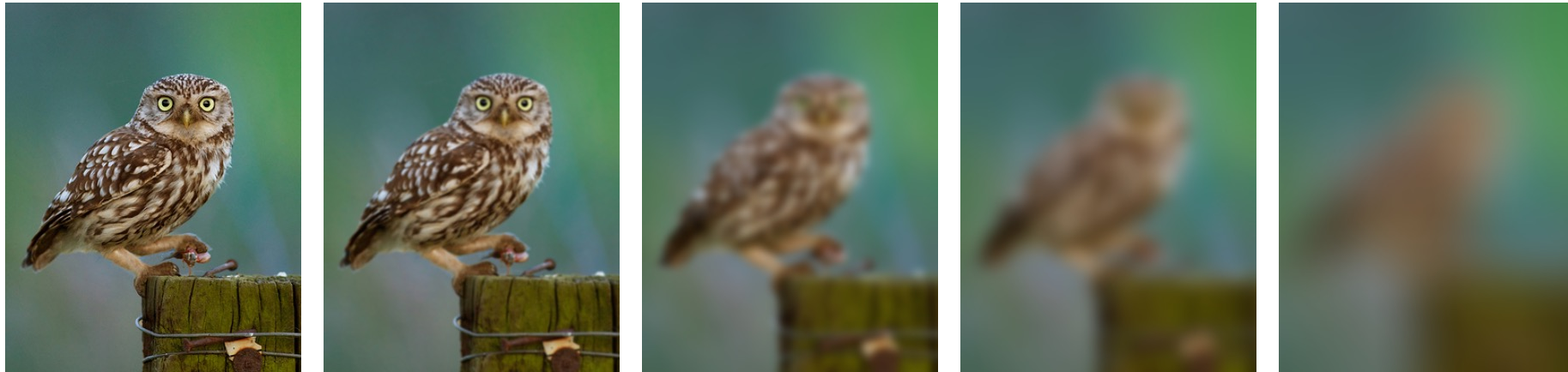


$$G_{\sigma} = \frac{1}{2\pi\sigma^2} e^{-\frac{(x^2+y^2)}{2\sigma^2}}$$

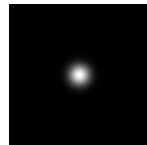
- If a neighboring pixel is closer to the current pixel, it will be assigned a larger weight
- The  $\sigma$  controls the width of the kernel

Source: C. Rasmussen

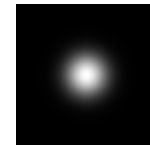
# Gaussian filters



$\sigma = 1$  pixel



$\sigma = 5$  pixels



$\sigma = 10$  pixels

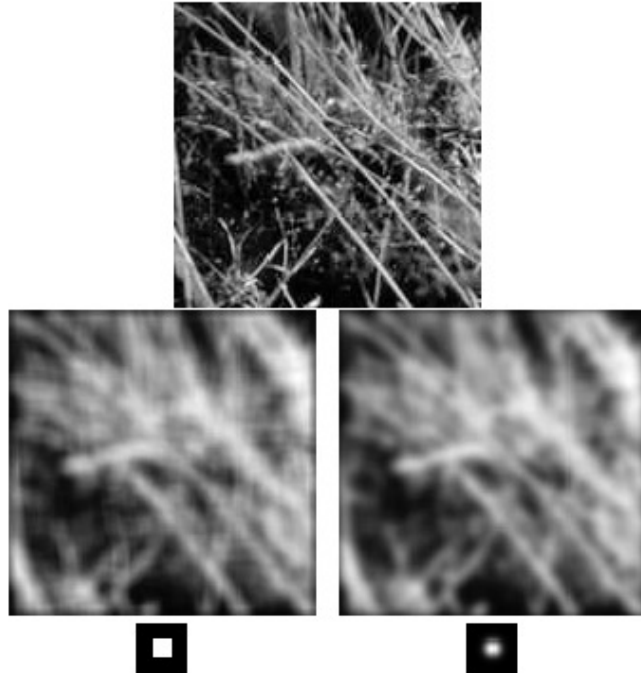


$\sigma = 30$  pixels

A Gaussian filter with a larger  $\sigma$  will produce a more blurred image

Slide credit: N. Snavely

# Mean vs. Gaussian filtering

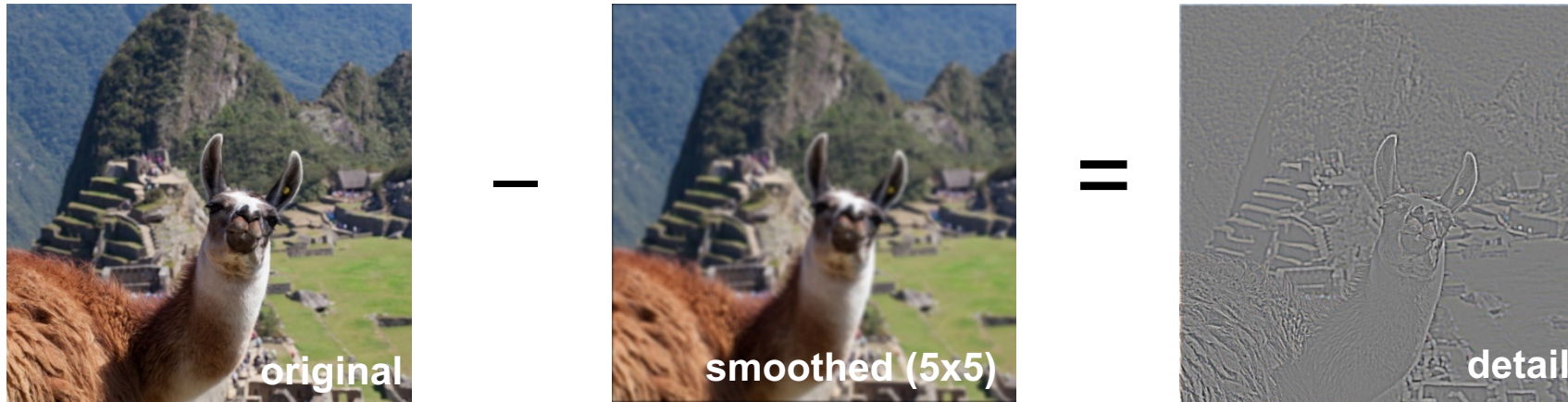


Both mean and Gaussian utilize local smoothness prior

- Mean filter assumes all pixels in a local window are equally important
- Gaussian filter assumes pixels that are closer to the target pixel are more important

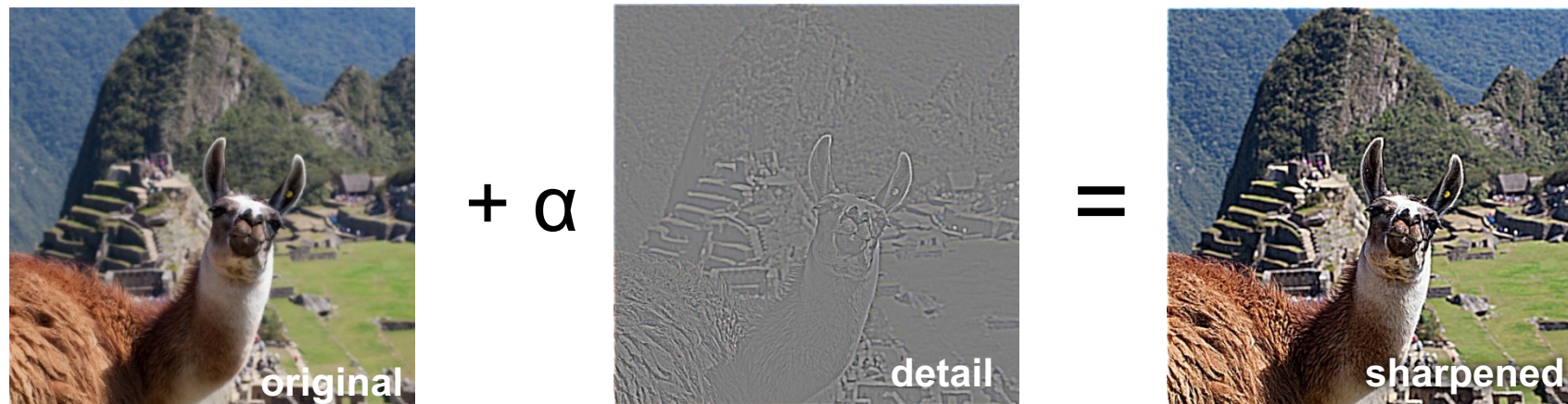
Source: N. Snavely

# Sharpening revisited: What does blurring take away?



(This “detail extraction” operation is also called a *high-pass filter*)

Let's add it back:



Slide credit: N. Snavely

Filtered Image



Noisy Image



Question: How to handle blurry artifacts and preserve high-frequency details in the filtered image?

Nonlocal Means Filtering



Noisy Image

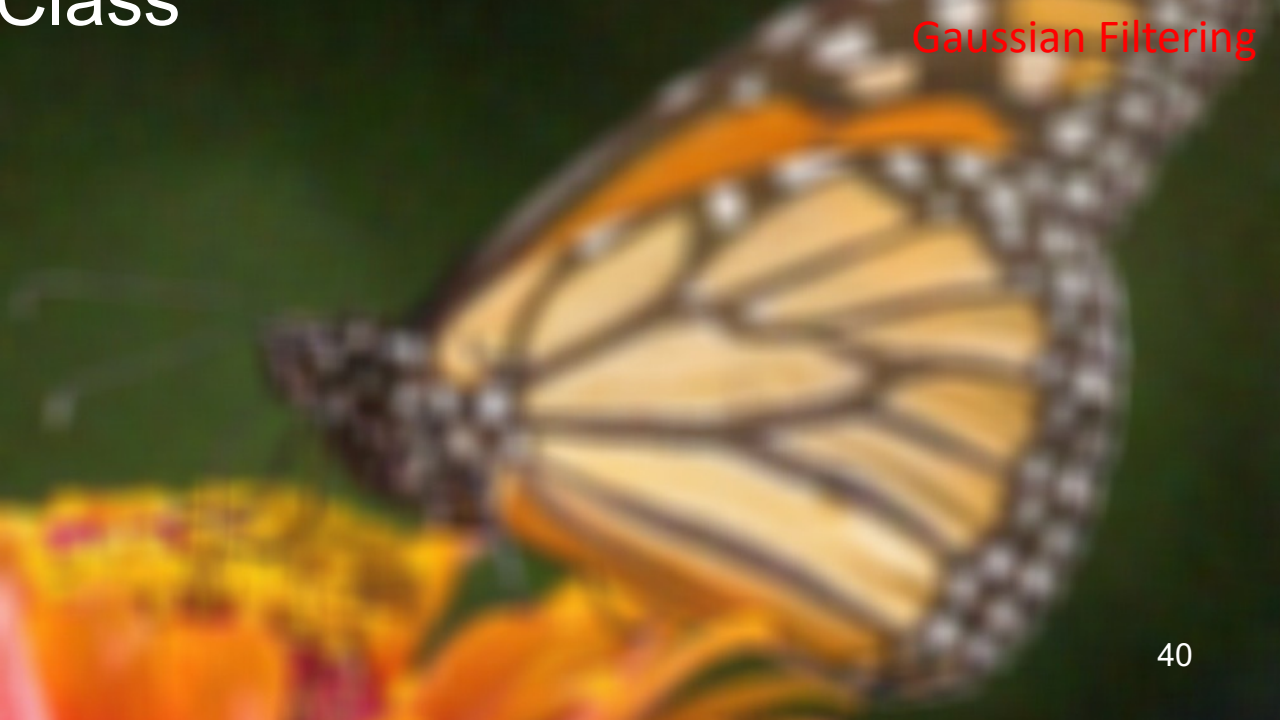


Next Class

Bilateral Filtering



Gaussian Filtering





# Further Reading

Chapters 3.1 and 3.2, Computer Vision: Algorithms and Applications,  
Richard Szeliski